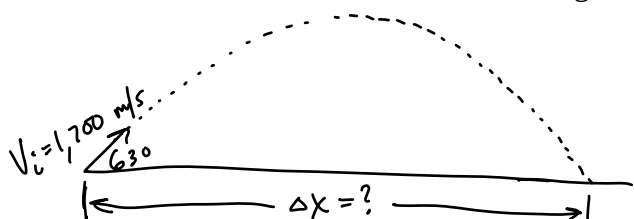


Name: KEY
 Date: _____
 Section C D F

Projectile Motion II - Angled

1. A ball is fired from the ground with an initial speed of 1.70×10^3 m/s (approximately five times the speed of sound) at an initial angle of 63.0° to the horizontal. Neglect air resistance.

a. Find the ball's horizontal range.



$$\begin{aligned} \Delta x &= 238,401 & \Delta y &= 0 \\ V_{ix} &= 772 & V_{iy} &= 1515 \\ V_{fx} &= 772 & V_{fy} &= \\ a &= 0 & a &= 9.81 \text{ m/s}^2 \\ \Delta t &= & \Delta t &= 309 \text{ s} \end{aligned}$$

$$\Delta y = (V_{iy} \sin \theta) \Delta t - \frac{1}{2} g \Delta t^2$$

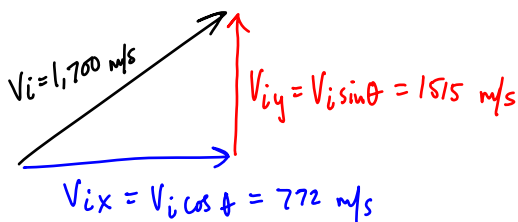
$$0 = 1515 \Delta t - (4.905) \Delta t^2$$

$$4.905 \Delta t^2 = 1515 \Delta t$$

$$4.905 \Delta t = 1515$$

$$\Delta t = 309 \text{ s}$$

b. Find the amount of time the ball is in motion.

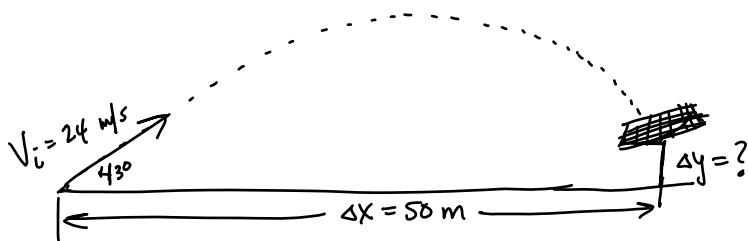


$$\Delta x = V_x \Delta t$$

$$\Delta x = (772)(309)$$

$$\Delta x = 238,401 \text{ m}$$

2. A daredevil is shot out of a cannon at 43.0° to the horizontal with an initial speed of 24.0 m/s. A net is positioned a horizontal distance of 50.0 m from the cannon. At what height above the cannon should the net be placed in order to catch the daredevil?



$$\begin{aligned} \Delta x &= 50 \text{ m} & \Delta y &= ? \\ V_{ix} &= 17.55 & V_{iy} &= 16.37 \\ V_{fx} &= 17.55 & V_{fy} &= 16.37 \\ a &= & a &= 9.81 \text{ m/s}^2 \\ \Delta t &= & \Delta t &= \end{aligned}$$

$$\Delta x = V_x \Delta t$$

$$\Delta t = \frac{\Delta x}{V_x} = \frac{50}{17.55}$$

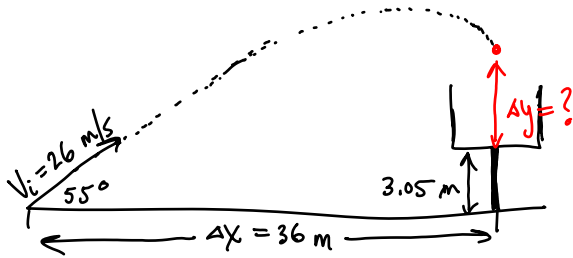
$$\Delta t = 2.85 \text{ sec}$$

$$\Delta y = V_{iy} \sin \theta \Delta t - \frac{1}{2} g \Delta t^2$$

$$\Delta y = 6.808 \text{ m}$$

3. A place kicker must kick a football from a point 36.0 m (about 40.0 yd) from the goal, and the ball must clear the crossbar, which is 3.05 m high. When kicked, the ball leaves the ground with a speed of 26.0 m/s at an angle of 55° to the horizontal.

a. By how much does the ball clear the crossbar?



$$\begin{aligned} \Delta x &= 36 \text{ m} & \Delta y &= ? & \Delta x &= v_x \Delta t \\ v_{ix} &= 14.91 & v_{iy} &= 21.30 & \Delta t &= 2.414 \text{ sec} \\ v_{fx} &= 14.91 & v_{fy} &= ? & \Delta y &= v_{iy} \Delta t - \frac{1}{2} g \Delta t^2 \\ a &= 0 & a &= 9.81 & \Delta y &= (21.3) \Delta t - 4.905 \Delta t^2 \\ \Delta t &= \Delta t & & & \Delta y &= 22.83 \text{ m} \end{aligned}$$

$$\Delta y - 3.05 \text{ m} = 19.78 \text{ m}$$

- b. Does the ball approach the crossbar while still rising or while falling? (Hint: If $v_{f,y}$ is positive, the ball is still rising, if $v_{f,y}$ is negative, the ball is falling)

$$v_{fy} = v_i \sin \theta - g \Delta t$$

$$v_{fy} = 21.30 - (9.81)(2.414)$$

$$v_{fy} = -2.38 \text{ m/s} \quad (\text{falling})$$

- c. What is the vertical component of velocity of the ball at this time?