

Name: KEY

Date: _____

Section C D F

Harmonic Motion 2Pendulum Oscillations

1. Find the period and frequency of a 9.8 m long pendulum. (2 pts)

$$T = 2\pi \sqrt{\frac{L}{g}}$$

$$T = 2\pi \sqrt{\frac{9.8}{9.81}}$$

$$T = 6.28 \text{ s}$$

$$F = \frac{1}{T}$$

$$F = \frac{1}{6.28}$$

$$F = .159 \text{ Hz}$$

2. A visitor to a lighthouse wishes to determine the height of the tower. The visitor ties a spool of thread to a small rock to make a simple pendulum, and then hangs the pendulum down a spiral staircase in the center of the tower. The period of oscillation is 9.49 s. What is the height of the tower? (2 pts)

isolate L

$$T = 2\pi \sqrt{\frac{L}{g}}$$

$$\frac{T}{2\pi} = \sqrt{\frac{L}{g}}$$

$$\left(\frac{T}{2\pi}\right)^2 = \frac{L}{g}$$

$$g \left(\frac{T}{2\pi}\right)^2 = L$$

$$L = 9.81 \left(\frac{9.49}{2\pi}\right)^2$$

$$L = 22.38 \text{ m}$$

3. A 3 m long pendulum on the moon takes 8.511 seconds to complete 1 pendulum. What is the value of gravity on the moon? (2 pts)

isolate g

$$T = 2\pi \sqrt{\frac{L}{g}}$$

$$\left(\frac{T}{2\pi}\right)^2 = \frac{L}{g}$$

$$g \left(\frac{T}{2\pi}\right)^2 = L$$

$$g = \frac{L}{\left(\frac{T}{2\pi}\right)^2}$$

$$g_{\text{moon}} = \frac{3}{\left(\frac{8.511}{2\pi}\right)^2}$$

$$g_{\text{moon}} = 1.635 \text{ m/s}^2$$

Spring-Mass Oscillations

4. A spring with a spring constant of $1.8 \times 10^2 \text{ N/m}$ is attached to a 1.5 kg mass and then set in motion. (2 pts)

a. What is the period of the mass-spring system?

$$T = 2\pi \sqrt{\frac{m}{k}}$$

$$T = 2\pi \sqrt{\frac{1.5}{180}}$$

$$T = .57 \text{ s}$$

b. What is the frequency of the vibration?

$$f = \frac{1}{T} = \frac{1}{.57} = 1.74 \text{ Hz}$$

5. Two teenagers take a big F-350 truck joyriding around an off-road race course, with a combined weight of 2450 kg . A jump in the course sends the truck jumping and upon landing the shocks in the car oscillate for 1.1 seconds . Find the spring constant of the shocks in the truck. (2 pts)

$$M = 2450$$

$$T = 1.1 \text{ seconds}$$

$$T = 2\pi \sqrt{\frac{m}{k}}$$

$$\left(\frac{T}{2\pi}\right)^2 = \frac{m}{k}$$

$$k \left(\frac{T}{2\pi}\right)^2 = m$$

$$k = \frac{m}{\left(\frac{T}{2\pi}\right)^2}$$

$$k = \frac{2450}{\left(\frac{1.1}{2\pi}\right)^2}$$

$$k = 8.00 \times 10^4 \text{ N/m}$$

Assuming 4 shocks (there are actually 7,
thanks Courtney + Julia)

$$\frac{k}{4} = 2.00 \times 10^4 \text{ N/m}$$